

Les vecteurs

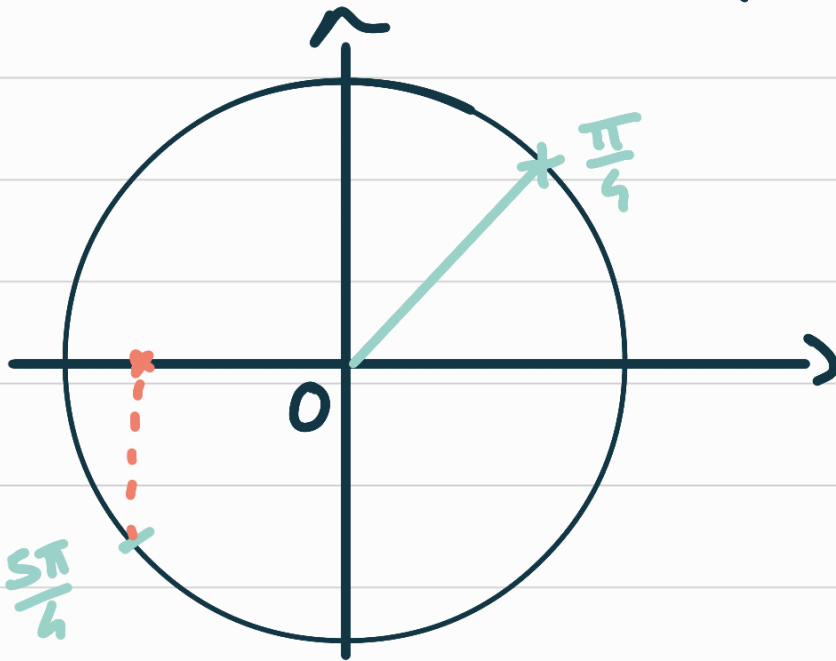
exercice :

$$\|\vec{u}\| = 6 \quad \|\vec{v}\| = 4$$

$$\text{et } (\vec{u}, \vec{v}) = \frac{5\pi}{4}.$$

Calculer le produit scalaire $\vec{u} \cdot \vec{v}$.

$$\vec{u} \cdot \vec{v} = 6 \times 4 \times \cos\left(\frac{5\pi}{4}\right)$$



$$\vec{u} \cdot \vec{v} = 6 \times \cancel{4} - \frac{\sqrt{2}}{\cancel{2}}$$

$$= -12\sqrt{2}.$$

exercice :

$$\vec{u}(2; 6) \quad \vec{v}(-3; 5)$$

1) Calculer $\|\vec{u}\|$, $\|\vec{v}\|$, $\|\vec{u} + \vec{v}\|$

$$\|\vec{u}\| = \sqrt{2^2 + 6^2} = \sqrt{4 + 36} = \sqrt{40}$$

$$\|\vec{v}\| = \sqrt{(-3)^2 + 5^2} = \sqrt{34}$$

$$\vec{u} + \vec{v} \quad (-1; 11)$$

$$\hookrightarrow \|\vec{u} + \vec{v}\| = \sqrt{(-1)^2 + 11^2} = \sqrt{122}$$

2) Calculer $\vec{u} \cdot \vec{v}$.

$$\vec{u} \cdot \vec{v} = \frac{1}{2} (\|\vec{u} + \vec{v}\|^2 - \|\vec{u}\|^2 - \|\vec{v}\|^2)$$

$$= \frac{1}{2} (122 - 40 - 34)$$

$$= \frac{1}{2} \times 48$$

$$= 24.$$

$$\vec{u} \cdot \vec{v} = \frac{1}{2} (\|\vec{u} + \vec{v}\|^2 - \|\vec{u}\|^2 - \|\vec{v}\|^2)$$

$$\vec{u} \cdot \vec{v} = \frac{1}{2} (\|\vec{u}\|^2 + \|\vec{v}\|^2 - \|\vec{u} - \vec{v}\|^2)$$

exercice :

$$A(-9; 4) \quad B(1; -1)$$

$$\text{et } C(4; -2).$$

Calculer $\vec{AB} \cdot \vec{AC}$.

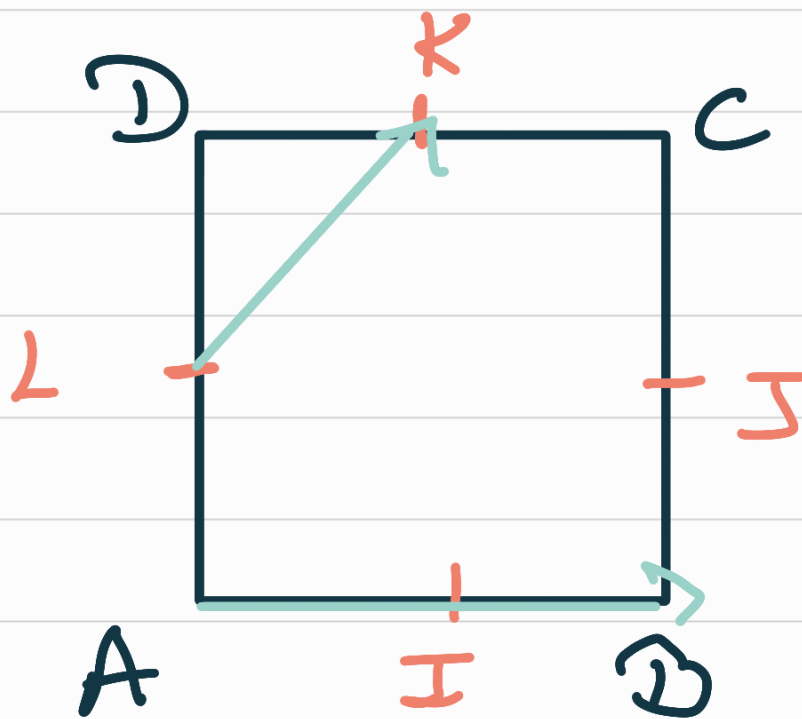
$$\vec{AB}(-10; -5) \quad \vec{AC}(13; -6)$$

$$\vec{AB} \cdot \vec{AC} = 10 \times 13 + (-5) \times (-6)$$

$$= 130 + 30$$

$$= 160.$$

exercice :



côté 1

$$\cdot \vec{BC} \cdot \vec{DL} = \vec{BC} \cdot \vec{BA} = 0$$

$$\cdot \vec{IB} \cdot \vec{ID} = \vec{IB} \cdot \vec{IA} = -IB \times IA$$

$$= -\frac{1}{2} \times \frac{1}{2} = -\frac{1}{4}$$

$$\cdot \vec{KJ} \cdot \vec{KL} = \vec{KC} \cdot \vec{KD} = -KC \times KD$$
$$= -\frac{1}{2} \times \frac{1}{2}$$

$$= -\frac{1}{4}.$$

$$\vec{AB} \cdot \vec{LK} = \vec{AB} \cdot \vec{AD} = 0$$

Exercice 3.

MNPQ est un carré avec $MN = 6$, I est le centre du carré.

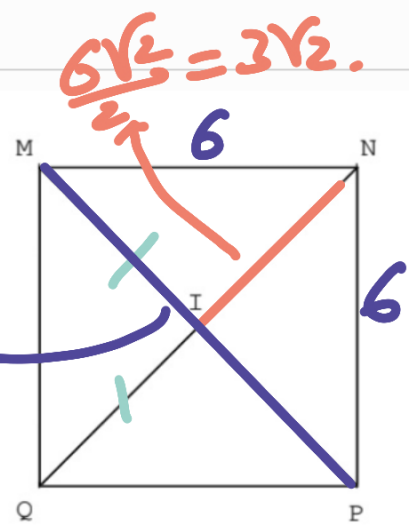
Calculer les produits scalaires suivants :

- 1) $\vec{MN} \cdot \vec{QP}$
- 2) $\vec{MN} \cdot \vec{PN}$
- 3) $\vec{IN} \cdot \vec{IP}$
- 4) $\vec{QI} \cdot \vec{NI}$

Pythagore

$$6^2 + 6^2 = 36 + 36 = 72$$

$$\Rightarrow \sqrt{72} = 6\sqrt{2}$$



$$\vec{MN} \cdot \vec{QP} = MN \times QP = 6 \times 6 = 36$$

$$\vec{MN} \cdot \vec{PN} = 0$$

$$\begin{aligned} \vec{IN} \cdot \vec{IP} &= IN \times -IQ \\ &= -IN \times IQ \\ &= -(3\sqrt{2}) \times (3\sqrt{2}) \\ &= -18 \end{aligned}$$

$$\bullet \vec{QI} \cdot \vec{NI} = QI \times -IN \\ = -18.$$

$$\vec{AB} = \vec{AC} + \vec{CB}$$